

# Statistics

## Lecture 11



Feb 19-8:47 AM

Class Quiz 2

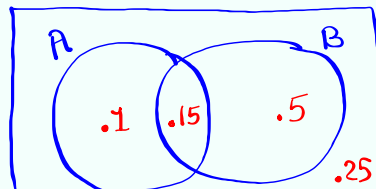
Given  $P(A) = .25$ ,  $P(B) = .65$ ,  $P(A \text{ and } B) = .15$ 

1)  $P(\bar{A}) = 1 - P(A)$

$= 1 - .25$

$= \boxed{.75}$

2) Construct Venn Diagram



3)  $P(A \text{ or } B)$

$= P(A) + P(B) - P(A \text{ and } B)$

$= .25 + .65 - .15 = \boxed{.75}$

4)  $P(A \text{ only OR } B \text{ only}) = .1 + .5 = \boxed{.6}$

5)  $P(\bar{A} \text{ and } \bar{B}) = P(\overline{A \text{ or } B}) = 1 - P(A \text{ or } B) = 1 - .75 = \boxed{.25}$

**De Morgan's Law**

6)  $P(\bar{A} \text{ or } \bar{B}) = P(\overline{A \text{ and } B}) = 1 - P(A \text{ and } B) = 1 - .15 = \boxed{.85}$

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Suppose  $P(A) = .4$ ,  $P(B) = .5$ ,  $A \text{ \& } B$  are M.E.E.  
disjoint events

1)  $P(\bar{A}) = 1 - .4 = \boxed{.6}$

2)  $P(A \text{ and } B) = \boxed{0}$

3)  $P(A \text{ or } B) = .4 + .5 - 0 = \boxed{.9}$

4) Draw Venn Diagram

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A box has 4 Quarters and 6 nickels.  
Take 2 Coins with replacement

$P(\text{Both Quarters}) = \frac{4}{10} \cdot \frac{4}{10} = \frac{2}{5} \cdot \frac{2}{5} = \frac{4}{25} = \boxed{.16}$

$P(\text{Both Nickels}) = \frac{6}{10} \cdot \frac{6}{10} = \frac{3}{5} \cdot \frac{3}{5} = \frac{9}{25} = \boxed{.36}$

$P(\text{one of each}) = 2 \cdot \frac{4}{10} \cdot \frac{6}{10} = \frac{48}{100} = \frac{12}{25} = \boxed{.48}$   
 QN or NQ      $48 \div 100$  Math  $\frac{12}{25}$  Enter

what if we take 3 coins with replacement

$P(\text{All Quarters}) = \frac{4}{10} \cdot \frac{4}{10} \cdot \frac{4}{10} = \frac{2}{5} \cdot \frac{2}{5} \cdot \frac{2}{5} = \frac{8}{125}$

$P(\text{All Nickels}) = \frac{6}{10} \cdot \frac{6}{10} \cdot \frac{6}{10} = \frac{3}{5} \cdot \frac{3}{5} \cdot \frac{3}{5} = \frac{27}{125}$

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Independent Events  
 $P(A \text{ and } B) = P(A) \cdot P(B)$

Dependent Events  
 $P(A \text{ and } B) = P(A) \cdot P(B|A)$

A full deck of playing cards has 52 cards, 12 face cards, and 4 aces.

Take two cards without replacement

$P(\text{Both Aces}) = \frac{4}{52} \cdot \frac{3}{51} = \frac{1}{13} \cdot \frac{1}{17} = \frac{1}{221}$   
 Rare event  $\approx 0.005$

$P(\text{Both Face Cards}) = \frac{12}{52} \cdot \frac{11}{51} = \frac{11}{221} \approx 0.050$

12  $\frac{12}{52}$  11  $\frac{11}{51}$  Math 1: Frc Enter

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A box has 7 nickels & 3 dimes.

Take 2 coins, No replacement

Tree Diagram

Sample Space

$P(NN) = \frac{7}{10} \cdot \frac{6}{9} = \frac{7}{15}$        $P(DD) = \frac{3}{10} \cdot \frac{2}{9} = \frac{1}{15}$

$P(ND) = \frac{7}{10} \cdot \frac{3}{9} = \frac{7}{30}$        $P(DN) = \frac{3}{10} \cdot \frac{7}{9} = \frac{7}{30}$

$\frac{7}{15} + \frac{1}{15} + \frac{7}{30} + \frac{7}{30} = 1$  Total Prob.

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4 Females , 8 Males , Select 3 people.

FFF

$$P(FFF) = \frac{4}{12} \cdot \frac{3}{11} \cdot \frac{2}{10} = \boxed{\frac{1}{55}}$$



$$P(MMM) = \frac{8}{12} \cdot \frac{7}{11} \cdot \frac{6}{10} = \boxed{\frac{14}{55}}$$

MMM

$$P(\text{Same Gender}) = P(\text{All Females or All Males})$$

$$= \frac{1}{55} + \frac{14}{55} = \frac{15}{55} = \boxed{\frac{3}{11}}$$

$$P(\text{Some F \& Some M}) = 1 - P(\text{Same gender})$$

$$= 1 - \frac{3}{11} = \boxed{\frac{8}{11}}$$

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4 Females , 8 Males , Select 3 people.

FFF

$$P(FFF) = \frac{4}{12} \cdot \frac{3}{11} \cdot \frac{2}{10} = \boxed{\frac{1}{55}}$$



$$P(MMM) = \frac{8}{12} \cdot \frac{7}{11} \cdot \frac{6}{10} = \boxed{\frac{14}{55}}$$

MMM

$$P(\text{at least 1 Female}) = 1 - P(\text{No Female})$$

$$= 1 - P(MMM) = 1 - \frac{14}{55} = \boxed{\frac{41}{55}}$$

$$P(\text{at least 1 Male}) = 1 - P(\text{No Males})$$

$$= 1 - P(\text{All Females})$$

$$= 1 - \frac{1}{55} = \boxed{\frac{54}{55}}$$

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$$P(A \text{ and } B) = P(A) \cdot P(B|A)$$

$$P(B|A) = \frac{P(A \text{ and } B)}{P(A)}$$

Conditional Prob.

$$P(A) = .4$$

$$P(B) = .5$$

$$P(A \text{ and } B) = .3$$

$$P(A|B) = \frac{P(A \text{ and } B)}{P(B)}$$

$$= \frac{.3}{.5} = \boxed{.6}$$

$$P(B|A) = \frac{P(A \text{ and } B)}{P(A)}$$

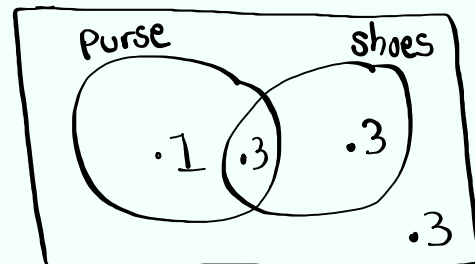
$$= \frac{.3}{.4} = \boxed{.75}$$

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$$P(\text{purse}) = .4$$

$$P(\text{shoes}) = .6$$

$$P(\text{Purse and Shoes}) = .3$$



$$P(\text{shoes} | \text{purse}) = \frac{P(\text{Purse and Shoes})}{P(\text{Purse})} = \frac{.3}{.4} = \boxed{.75}$$

$$P(\text{Purse} | \text{shoes}) = \frac{P(\text{Purse and Shoes})}{P(\text{Shoes})} = \frac{.3}{.6} = \boxed{.5}$$

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John went shopping.

$P(\text{shirt}) = .5$

$P(\text{Pants}) = .8$

$P(\text{shirt} | \text{Pants}) = .6$

$P(\text{Shirt and Pants}) = ?$

$P(\text{Shirt} | \text{Pants}) = \frac{P(\text{S and P})}{P(\text{Pants})}$

$.6 = \frac{P(\text{shirt and pants})}{.8}$

Cross-Multiply

$P(\text{S and P}) = (.6)(.8)$

$= .48$

$P(\text{He buys one of them, not both})$

$= .02 + .32 = .34$

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Introduction to Counting.

think of your password of

1) 4 digits

	$\frac{10}{\text{First \#}}$	$\frac{10}{\text{Second \#}}$	$\frac{10}{\text{Third \#}}$	$\frac{10}{\text{Fourth \#}}$
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when repetition is allowed

$10 \cdot 10 \cdot 10 \cdot 10 = 10,000$

No repetition

$10 \cdot 9 \cdot 8 \cdot 7 = 5040$

2) think of an ID

Have a letter, followed by 6 digits.

$26 \cdot 10 \cdot 10 \cdot 10 \cdot 10 \cdot 10 \cdot 10$

Letter  $\uparrow$   $52 \cdot 10 \cdot 9 \cdot 8 \cdot 7 \cdot 6 \cdot 5$

Case Sensitive  $\uparrow$

NO repetition.

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Roll a die, then flip a coin.

How many outcomes?

1H	1T	
2H	2T	
3H	3T	
⋮	⋮	
6H	6T	

$6 \cdot 2 = 12$   
 Total choices

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5 people  
 Adam    Bill    Carol    David    Eddie

Select 2 people

<del>AB</del>	<del>AC</del>	<del>AD</del>	<del>AE</del>	Total choices $5 \cdot 4 = 20$ what if order does not matter
BA	<del>BC</del>	<del>BD</del>	<del>BE</del>	
CA	CB	<del>CD</del>	<del>CE</del>	
DA	DB	DC	<del>DE</del>	
EA	EB	EC	ED	

10 choices

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$n^C_r$        $n$  choose  $r$   
 $n$  different items  
 Select  $r$  of them  
 order does not matter  
 NO replacement  
 $3! = 3 \cdot 2 \cdot 1 = 6$   
 $6! = 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 720$   
 6 [MATH] [→] PRB [↓] ! [Enter]  
 $10! = 3,628,800$   
 $50! \approx 3.04 \times 10^{64}$

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$5^C_2 = \frac{5!}{2! \cdot (5-2)!} = \frac{5!}{2! \cdot 3!} = \frac{5 \cdot \cancel{4} \cdot \cancel{3} \cdot \cancel{2} \cdot 1}{2 \cdot 1 \cdot \cancel{3} \cdot \cancel{2} \cdot 1} = 10$   
 5 [MATH] [→] PRB [↓] nCr 2 [Enter]

A basketball team has 15 players, but 5 should start the game.  
 How many ways can this happen?  
 $15^C_5 = 3003$

CA Lotto  
 50 numbers  
 choose 5 numbers  
 $50^C_5 = 2,118,760$

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4 Females , 8 Males

Select 3 people , No replacement, order does not matter.

1) How many ways can we do this?

$${}_{12}C_3 = \boxed{220}$$

2) How many ways can we select 3 Females?

$${}_{4}C_3 = 4$$

$$3) P(FFF) = \frac{{}_{4}C_3}{{}_{12}C_3} = \frac{4}{220} = \frac{1}{55}$$

$$4) P(MMM) = \frac{{}_{8}C_3}{{}_{12}C_3} = \frac{56}{220} = \boxed{\frac{14}{55}}$$

$$5) P(2F \& 1M) = \frac{{}_{4}C_2 \cdot {}_{8}C_1}{{}_{12}C_3} = \frac{48}{220} = \boxed{\frac{12}{55}}$$

$$6) P(1F \& 2M) = \frac{{}_{4}C_1 \cdot {}_{8}C_2}{{}_{12}C_3} = \frac{112}{220} = \boxed{\frac{28}{55}}$$

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